

# Serial Effects are optimal

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Behavioral and Brain Sciences, Volume 41, 2018 , e229

<https://doi.org/10.1017/S0140525X18001395>

## Abstract

In the target article, Rahnev & Denison (R&D) use serial effects as an example of suboptimality. We show here that serial effects can be beneficial to perception, serving to reduce both error and response times in a near-optimal fashion. Furthermore, serial effects for stable attributes are positive, whereas those for changeable attributes are negative, demonstrating that they are engaged flexibly to optimize performance.

We read with great interest the article by Rahnev & Denison (R&D), reporting both a wide coverage of the issue of optimality in perception, as well as the many instances in which optimality has been hard to prove. One example of non-optimality for the authors is *serial dependence*, the influence of previous stimuli on current responses, in a sequential task (Burr & Cicchini [2014](#); Cicchini et al. [2014](#); Cicchini & Kristjánsson [2015](#); Fischer & Whitney [2014](#); Frund et al. [2014](#); Liberman et al. [2014](#)). The authors speculate that because the experimental setting prescribes independence between trials, it is suboptimal to carry over information from the previous trial. The only possibility they see is that perhaps the perceptual system is attuned to a general rule of continuity, which accidentally spills over into laboratory performance.

We encountered serial effects while studying perception of numerosity, finding that subjects were strongly biased toward the previous estimate, by up to 20% (Cicchini et al. [2014](#)). Importantly, at higher numerosities – where sensory resolution is lower – the serial effects were larger. This prompted us to investigate the effect with a standard Bayesian model in which the previous sensory experience can be considered an extra source of information ([Fig. 1](#)).

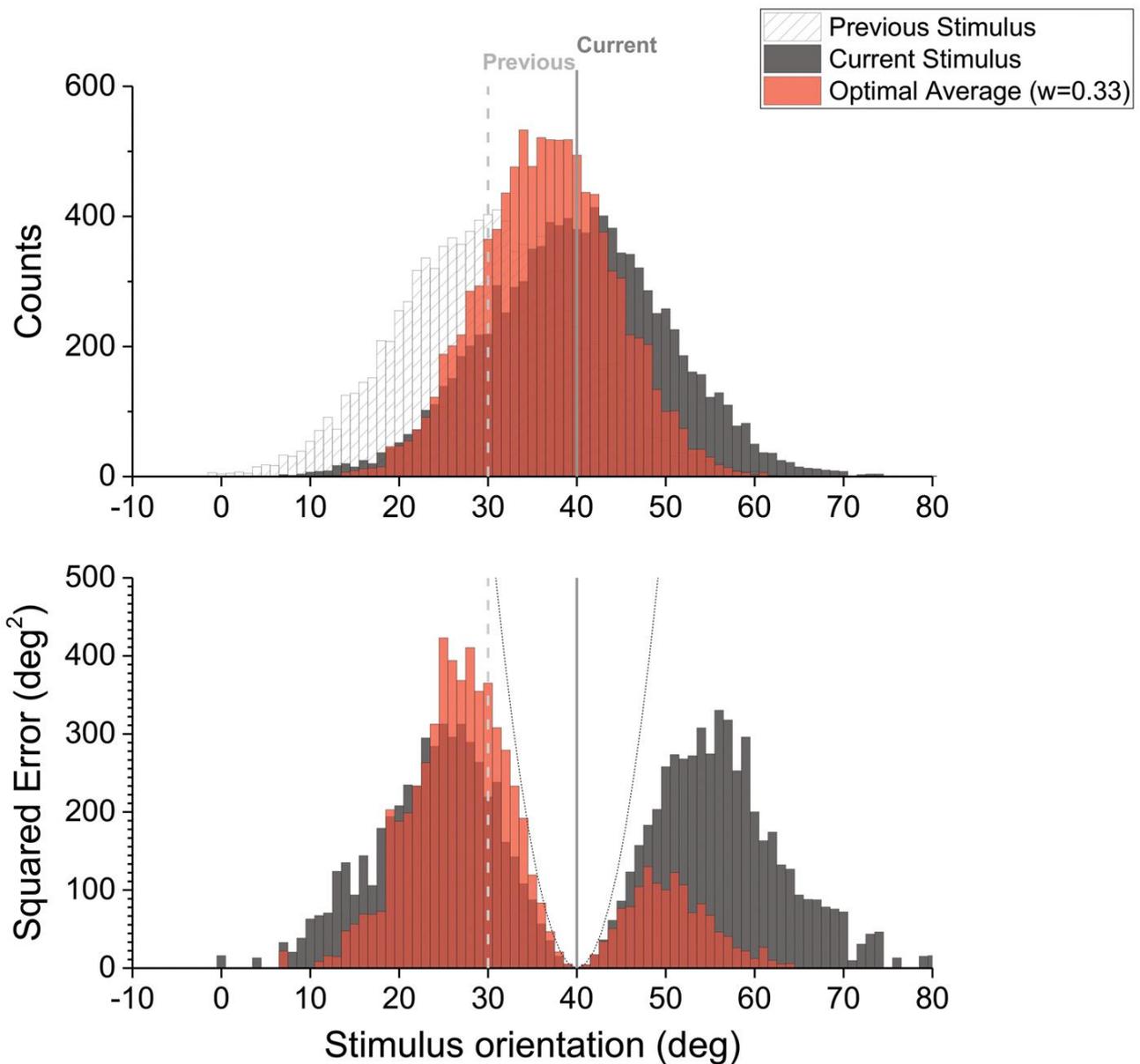


Figure 1. Serial dependence can be optimal. We illustrate the behavior of a noisy observer ( $\sigma = 10^\circ$ ) who is bound to estimate a stimulus at  $40^\circ$  orientation and can make optimal use of the previous trial which was at  $30^\circ$ . Response distributions are displayed in the top panel (black, memoryless model; red, model with serial dependence) and show a slight shift of responses toward the previous trial with a tightening of the distribution. Bottom panel shows the histograms of squared error cost: The overall error of the model taking advantage of serial dependencies is smaller than that of the memoryless model.

Simulations show that in the case of similar successive stimuli, this strategy is beneficial, as the uncertainty associated with the current judgment may benefit from integrating information from the past. According to our model, previous sensory experience should be weighted, taking into account the sensory resolution of the current and previous stimulus ( $\sigma_{curr}$ ,  $\sigma_{prev}$ ) along with the difference in

intensity between two presentations ( $d$ ):  $w_{prev} = \frac{\sigma_{curr}^2}{\sigma_{curr}^2 + \sigma_{curr}^2 + d^2}$ . This simple rule states that whenever there is multiple, congruent information, it is beneficial to blend it, without needing assumptions of continuity or meta-priors.

This model of optimal performance provided a good fit to the numerosity data set (Cicchini et al. [2014](#)). We went on to apply it successfully to orientation reproduction tasks (Cicchini et al. [2017](#); Cicchini et al. [2018](#)). In this experiment, we collected individual measures of precision and predicted (with zero degree of freed model and no further assumptions) subject behavior, obtaining an excellent fit both of the amount of serial dependence, as well as the range of orientation differences over which the effect occurs (Cicchini et al. [2018](#)). With the same data set, we also measured the benefit of serial dependence. We compared trials that were preceded by an identical stimulus (maximal dependence) and those preceded by a stimulus 45 degrees apart (when serial dependence waned). As predicted, we found a reduction of the squared error, about 45%, when serial dependence was maximal. We also compared response times and found that they were up to 60 ms faster for identical than for differing preceding stimuli. Overall, the two results show that the serial presentation of similar stimuli led to a genuine increase of information in the system. This latter result was totally unexpected as our model was developed starting from optimal cue integration literature (Alais & Burr [2004](#); Beierholm et al. [2008](#); Cicchini et al. [2012](#); Ernst & Banks [2002](#); Jazayeri & Shadlen [2010](#); Roach et al. [2006](#)) and was meant to optimize response error without considering time limits.

A final example that serial dependence does not result merely from a passive, no-optimal stickiness of the system is the demonstration that stimuli can induce either positive or negative serial dependencies, depending on their usefulness to the task in hand. Taubert et al. ([2016](#)) asked subjects to judge both the gender and expression (happy/sad) of sequentially presented faces. Strong positive serial dependence was found for gender – a stable attribute of a face that does not change over time. In the same experiment, with the same face stimuli, negative serial dependence was observed for expression, a labile attribute that changes frequently and rapidly, where the information is often in the change. Carrying over signals of expression from previous exposure would be of little help for the task in hand, and the system does not do it. This is a very clear demonstration that serial dependence is not an automatic result of the sluggishness of the system, but an active and flexible strategy to improve, and possibly optimize, perception.

Overall, we believe that the Bayesian framework has several merits for brain science. First, it encourages researchers to think of the brain as a statistical observer who accumulates information, and second, because it has helped to discover several strategies to obtain the same performance with fewer resources, such as removal of redundancy from retinal images to be transmitted via a small optic nerve. We agree with the authors that optimality is a loose concept and cannot be the only principle working in the brain; however, it has proved to provide an excellent framework with which to uncover the mechanisms of an organism that started evolving 200 million years ago.

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